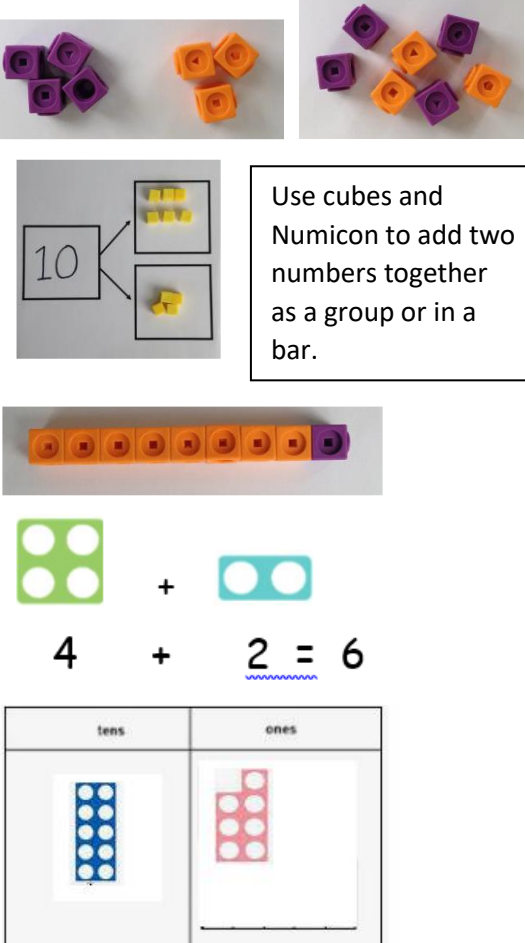
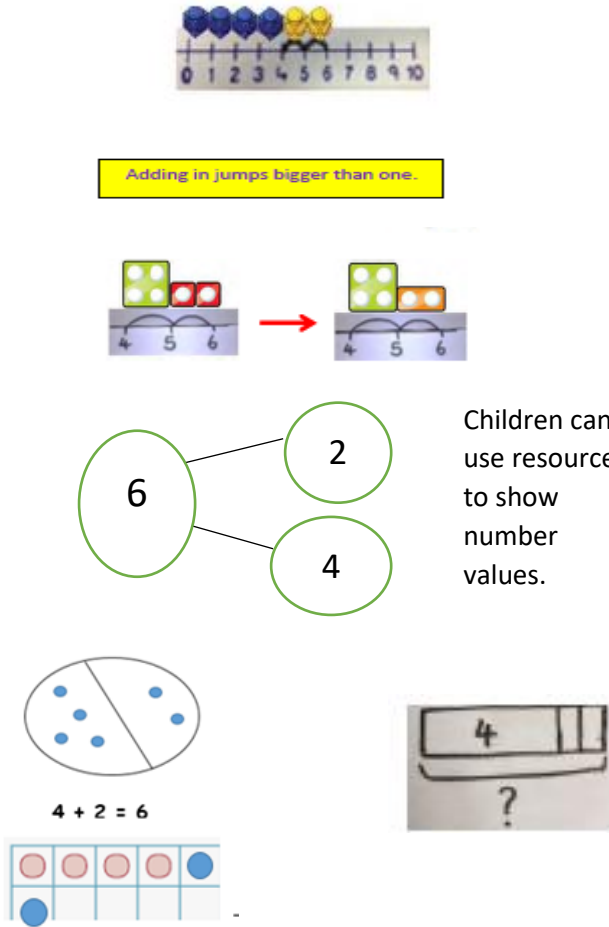


EYFS Addition

Strategies -

Early Learning Goal: Children to count reliably with numbers one to 20, place them in order and say which number is one more or one less than a given number. Using quantities and objects, they add and subtract two single-digit number and count on or back to find the answer.

Count on from the first group to add two groups of objects.

Language	Concrete	Pictorial	Abstract
<p>Plus Add More Total Altogether Make How many more...?</p>	 <p>Use cubes and Numicon to add two numbers together as a group or in a bar.</p> <p>4 + 2 = 6</p> <p>Show the value of digits using a place value grid</p>	 <p>Adding in jumps bigger than one.</p> <p>Children can use resources to show number values.</p> <p>4 + 2 = 6</p>	<p>Children will annotate concrete and pictorial images with numerals as they develop this skill. To support the recording of maths number stories will form an integral part of the teaching of maths. Children will then have an opportunity for independent recording at the maths writing table.</p>

1 Addition

National Curriculum

- Read, write and interpret mathematical statements involving addition (+) and equals (=) signs – This means the same as – relate this to balance number sentences and scales.
- Represent and use number bonds and related subtraction facts within 20.
- Add one-digit and two-digit numbers to 20, including zero
- Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as $9 = \square + 7$

Vocabulary	Concrete	Pictorial	Abstract
<p>Number bonds Number line Add Addition More Plus Make Sum Total Altogether Equals How many more? How many more is ... than ... Part/Whole Commutative Law</p>	<div data-bbox="376 454 627 790"> <p>Using Numicon to investigate the creation of 10 and above. First steps to bridging.</p> </div> <div data-bbox="403 805 828 933"> <p>$9 + 5 = 14$</p> </div> <div data-bbox="380 1029 616 1228"> <p>Start with the bigger number (9) add to make 10 (1), then add the remaining smaller number (4)</p> </div> <div data-bbox="403 1260 627 1436"> </div>	<p>Counting on: Learning that starting from the larger number is more efficient</p> <p>$15 = 12 + 3$</p> <div data-bbox="1086 614 1411 774"> </div> <p>The Power of 10 :Use pictures or a number line. Regroup or partition the smaller number to make 10.</p> <p>$9 + 5 = 14$</p> <div data-bbox="929 885 1512 1005"> </div> <div data-bbox="929 1021 1299 1252"> <p>Part-Part Whole Use this, as a way of showing addition is commutative: $9 + 5 = 14$ $5 + 9 = 14$ Progress to show = means the same as and move the = symbol $? = 6 + 3$</p> </div> <div data-bbox="940 1268 1198 1380"> </div>	<p>$17 = 5 + 12$</p> <p>Place the larger number in your head and count on the smaller number to find the answer.</p> <p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10. How many more do I add on now?</p> <p>$5 + 9 = 14$ $9 + 1 = 10$ $10 + 4 = 14$</p> <p>If I have nine, how many more do I need to make 10? How many more do I add on now?</p> <p>Commutative Law – Addition can be done in any order</p> <p>$15 + 1 = 1 + 15$</p>

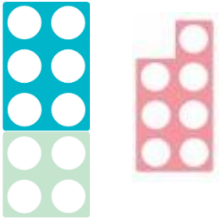

Year 2 Addition

National Curriculum:

Solve Problems with Addition:

- Using concrete objects and pictorial representations, including those involving number, quantities and measures
- Applying their increasing knowledge of mental and written methods
- Recall and use addition facts to 20 fluently, and derive and use related facts up to 100
- Add numbers using concrete object. Pictorial representation, and mentally, including:
 - A two digit number and ones
 - A two digit number and tens
 - 2 two digit numbers
 - Adding 3 one digit numbers
- Show the addition of two numbers can be done in any order (commutative) and subtraction from one number from another cannot.
- Recognise and use the inverse relationship between addition and subtraction and use this to check calculations, and solve missing number problems.

Adding 3 single digit numbers

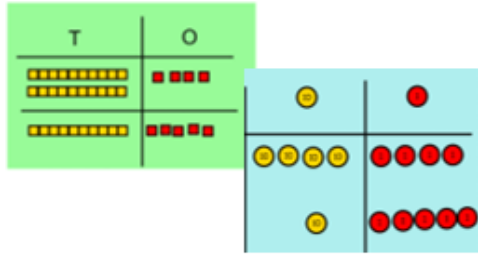
Vocabulary	Concrete	Pictorial	Abstract
Add Addition More Plus Make Sum Total Altogether Equals Is the same as Tens boundaries Number Line Part/Whole Bar Model Expanded Place Value column Operation Symbols Commutative Law	$4 + 7 + 6 = 17$ Put 4 and 6 together to make 10. Add on 7.  $4 + 6 + 7$ Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	 Add together three groups of objects. Draw a picture to recombine the groups to make 10.	$4 + 7 + 6 = 10 + 7$ $= 17$ Combine the two numbers that make 10 and then add on the remainder.

Adding two 2 digit numbers up to 100 without regrouping

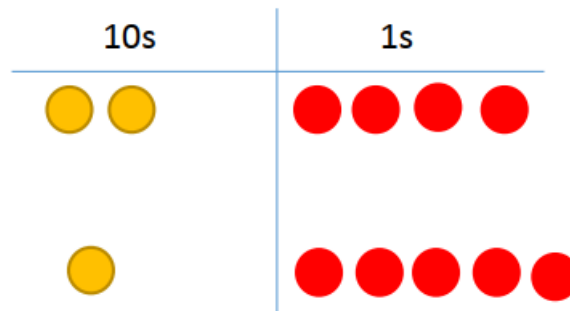
Use manipulatives to secure understanding of crossing 10's boundaries.

$$24 + 15 =$$

Add together the ones first then add the tens.
Use dienes first before moving onto place value counters



After physically using the dienes and place value counters, children can draw the counters to help them solve additions.



Year 2: Partition and Expanded method

$$\begin{array}{r} \text{T O} \quad \text{T O} \\ 44 + 15 \\ \hline 40 \quad 4 \\ + 10 \quad 5 \\ \hline 50 \quad 9 \end{array}$$

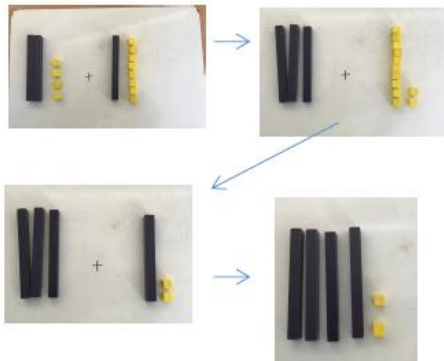
Not crossing 10's boundaries

Adding two 2 digit numbers up to 100 with regrouping

Use manipulatives to secure understanding of crossing 10's boundaries.

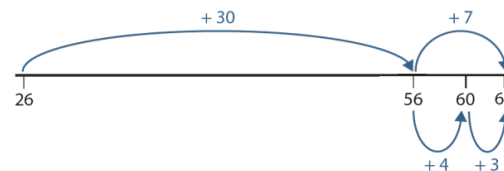
$$24 + 18 = 42$$

Add together the ones first then add the tens.
Develop to include regrouping.



26	37
----	----

$$26 + 37 = 26 + 30 + 7 = 63$$



Year 2: Partition and Expanded method – crossing 10's

Year 2: Expanded and column methods to add 2 digit numbers bridging 10

$$\begin{array}{r} \text{T O} \quad \text{T O} \\ 26 + 18 \\ \hline 20 \quad 6 \\ + 10 \quad 8 \\ \hline 40 \quad 4 \\ 10 \end{array}$$

Year 2: Partitioning both addends

$$\begin{array}{r} 26 \\ \swarrow \searrow \\ 20 \quad 6 \end{array} + \begin{array}{r} 37 \\ \swarrow \searrow \\ 30 \quad 7 \end{array}$$

$$20 + 30 = 50$$

$$6 + 7 = 13$$

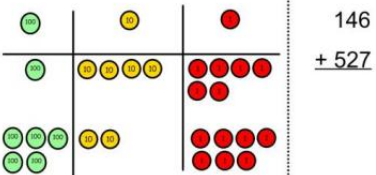
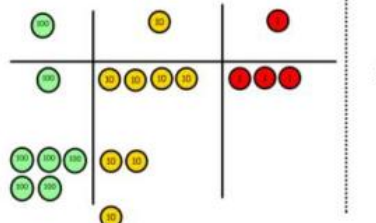
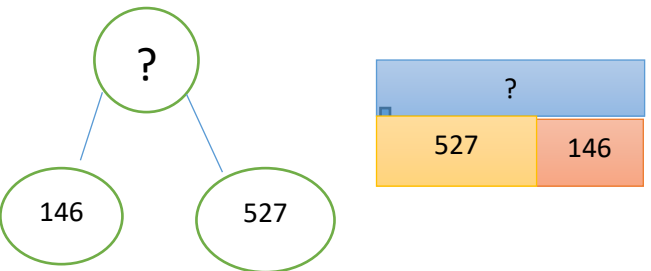
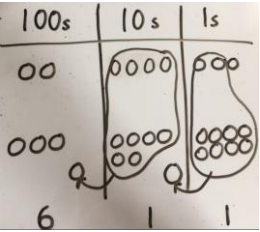
$$50 + 13 = 63$$

Year 3 Addition

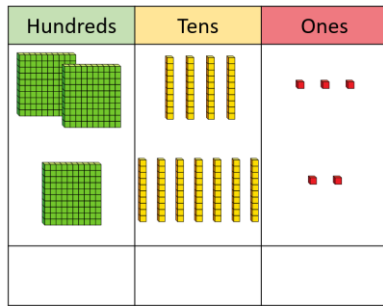
National Curriculum

Pupils should be taught to:

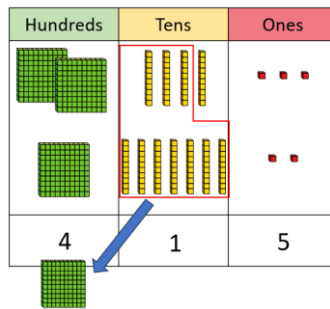
- Add numbers mentally including
- A 3 digit number and ones
- A 3 digit number and tens
- A 3 digit number and hundreds
- Add numbers up to 3 digit using formal written methods- column addition
- Estimate the answer to a calculation and use inverse operation to check answers
- Solve problems including missing number problems using number facts, place value and more complex addition

Vocabulary	Concrete	Pictorial	Abstract																				
Add 3 digit numbers with regrouping																							
<p>Addition / Add Plus/ More Sum/ Total/ Make Double Near Double Addend One more Ten more Hundred more How many more to make.... How many more is ... than... How much more is... Tens boundary Hundreds boundary Equals same as Operation sign Mental Calculation Equation Number Sentence Increase Greater than</p>	<p>Make both numbers on a place value grid with regrouping</p>  <p>Begin in the ones column. For every 10 created exchange for a 10 counter.</p> 	 <p>The part whole model and the bar model are used to reinforce the relationship between the Whole and the two parts. Addend + Addend = Sum</p> <p>Children also move from the manipulatives to drawing their own representations on a place value grid. Children to represent the counters in a place value chart, circling when they make an exchange.</p> 	<p>Expanded Written Method Leading to formal compact column method.</p> <p>Note that place value headings must be shown in compact method.</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td></td> <td>H</td> <td>T</td> <td>O</td> </tr> <tr> <td></td> <td>1</td> <td>4</td> <td>6</td> </tr> <tr> <td>+</td> <td>5</td> <td>2</td> <td>7</td> </tr> <tr> <td></td> <td>6</td> <td>7</td> <td>3</td> </tr> <tr> <td></td> <td></td> <td></td> <td>1</td> </tr> </table>		H	T	O		1	4	6	+	5	2	7		6	7	3				1
	H	T	O																				
	1	4	6																				
+	5	2	7																				
	6	7	3																				
			1																				

$$243 + 172 =$$

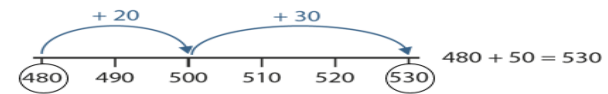
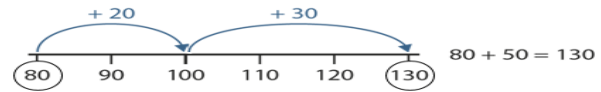


$$243 + 172 = 415$$



Dienes and Base Ten can also be used show making 10, 100, 1000.

Number Lines to aid fluency



Children to make the next 10 or 100 depending on context.

	H	T	O
	2	4	3
+	1	7	2
	4	1	5
	1		

Year 4 Addition

National Curriculum

Pupils should be taught to

- Add with up to 4 digits using the formal written methods of column addition and subtraction where appropriate.
- Estimate and use inverse operations to check answers to a calculation
- Solve addition two step-word problems in contexts, deciding which operations and methods to use and why.

Vocabulary

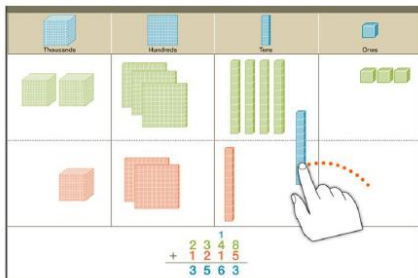
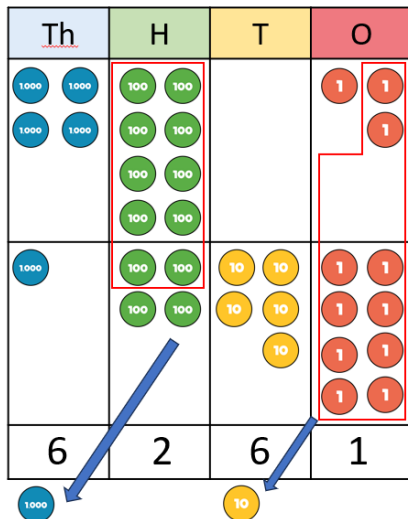
Concrete

Pictorial

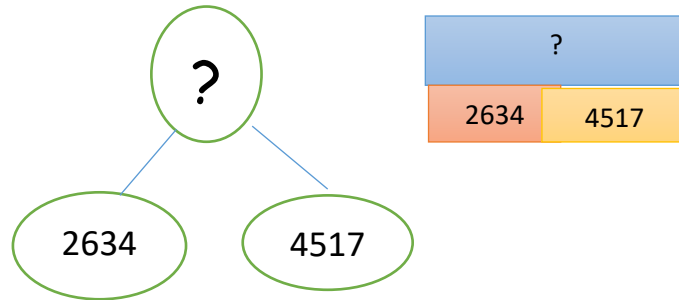
Abstract

See year 3

Include place value of thousands.
Include Tenths and Hundredths.

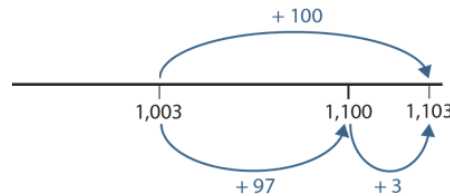


Use concrete materials to support conceptual understanding. Place value counters and frames are adapted to incorporate decimals.



Children to be able to record pictorially

$$1,003 + 100 = 1,103$$



Use of number lines to promote fluency and consolidation of place value.

Formal Compact Column Method.

	4	8	0	3	
+	1	4	5	8	
	6	2	6	1	
	1		1		

Year 5 Addition

National Curriculum

- Add whole numbers with more than 4 digits, including using column addition where appropriate.
- Add numbers mentally with increasingly large numbers
- Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy
- Solve addition multi-step problems in context, deciding which operations and methods to use and why.

Language

Enactive

Iconic

Symbolic

See previous years.

10,000s	1,000s	100s	10s	1s
3	8	4	0	1
0	2	6	1	7
+				
0	0	0	0	0
0	2	6	1	7

Tree diagram: $60 + 59 + 60 = 179$

Bar model: $60 + 59 + 60 = 179$

Number line: $3 + 9 = 12$

Thermometers: Day 9°C , Night -3°C

Number lines still have a place to promote fluency.

Symbolic representation of the addition:

$$38,401 + 2,617 =$$

3	8	4	0	1	
					=
+	2	6	1	7	
4	1	0	1	8	
1	1				

The use of place value headings is at the teacher's discretion.

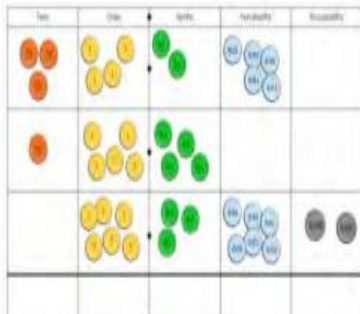
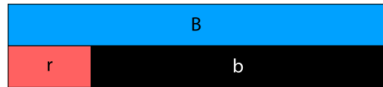
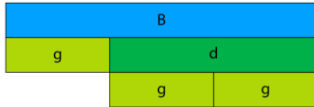

Year 6 Addition

National Curriculum

Pupil should be taught to:

- Solve addition multi-step problems in contexts, deciding which operations and methods to use and why.

Pupils should build on Year 5 strategy for addition when adding more than two numbers including numbers to three decimal places.

Language	Enactive	Iconic	Symbolic																																																																													
<p>When working with larger numbers model the correct placement of the comma: 1,678,029 Check children can confidently read these numbers</p>		<p>See previous years for iconic representations.</p> <div style="display: flex; justify-content: space-between; margin-bottom: 20px;"> <div data-bbox="936 603 1317 750">  <p>$B = r + b$</p> </div> <div data-bbox="1355 574 1601 710"> <p>Two unknowns; several solutions: I am thinking of two rods that together are equivalent to blue. What are they?</p> </div> </div> <div style="display: flex; justify-content: space-between; margin-bottom: 20px;"> <div data-bbox="936 901 1249 1045">  <p>$B = g + d$ $d = 2 \times g$</p> </div> <div data-bbox="1344 869 1579 1101"> <p>Two unknowns: one solution (multiplicative relationship between the unknowns): I am thinking of two rods that together are equivalent to blue. One is twice as long as the other. What are they?</p> </div> </div> <div style="display: flex; justify-content: space-between;"> <div data-bbox="936 1197 1288 1380">  <p>$B = p + y$ $y - p = w$ $p + w = y$</p> </div> <div data-bbox="1332 1197 1601 1404"> <p>Two unknowns; one solution (additive relationship between the unknowns): I am thinking of two rods that together are equivalent to blue. There is a difference of white between the two rods. What are they?</p> </div> </div>	<div style="text-align: center; margin-bottom: 20px;"> <table style="border-collapse: collapse; margin: auto;"> <tr><td style="padding: 0 10px;">1</td><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">0</td><td style="padding: 0 10px;">5</td><td style="padding: 0 10px;">3</td><td style="padding: 0 10px;">7</td></tr> <tr><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">3</td><td style="padding: 0 10px;">4</td><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">7</td><td style="padding: 0 10px;">1</td></tr> <tr><td style="padding: 0 10px;">+</td><td style="padding: 0 10px;">3</td><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">3</td><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">2</td></tr> <tr><td colspan="6" style="border-top: 1px solid black;"></td></tr> <tr><td style="padding: 0 10px;">6</td><td style="padding: 0 10px;">7</td><td style="padding: 0 10px;">8</td><td style="padding: 0 10px;">0</td><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">9</td></tr> <tr><td colspan="6" style="border-top: 1px solid black;"></td></tr> <tr><td></td><td style="text-align: center;">↑</td><td></td><td style="text-align: center;">↑</td><td></td><td></td></tr> </table> </div> <div style="text-align: center; margin-bottom: 20px;"> <table style="border-collapse: collapse; margin: auto;"> <tr><td style="padding: 0 10px;">0</td><td style="padding: 0 10px;">•</td><td style="padding: 0 10px;">5</td><td style="padding: 0 10px;">5</td><td style="padding: 0 10px;">7</td></tr> <tr><td style="padding: 0 10px;">1</td><td style="padding: 0 10px;">•</td><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">1</td><td style="padding: 0 10px;">1</td></tr> <tr><td style="padding: 0 10px;">+</td><td style="padding: 0 10px;">0</td><td style="padding: 0 10px;">•</td><td style="padding: 0 10px;">2</td><td style="padding: 0 10px;">0</td></tr> <tr><td colspan="5" style="border-top: 1px solid black;"></td></tr> <tr><td style="padding: 0 10px;">1</td><td style="padding: 0 10px;">•</td><td style="padding: 0 10px;">9</td><td style="padding: 0 10px;">7</td><td style="padding: 0 10px;">0</td></tr> <tr><td colspan="5" style="border-top: 1px solid black;"></td></tr> <tr><td></td><td></td><td style="text-align: center;">↑</td><td></td><td></td></tr> </table> </div> <p>Note in the example, the use of '0' as a place value holder here and as a digit within the decimal number itself: to reiterate the understanding of its importance and 'value'.</p>	1	2	0	5	3	7	2	3	4	2	7	1	+	3	2	3	2	2							6	7	8	0	2	9								↑		↑			0	•	5	5	7	1	•	2	1	1	+	0	•	2	0						1	•	9	7	0								↑		
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